## MATH 105

Probability Distributions and Expected Value

1. A fair die is rolled. The number (of dots) displayed on the top face of the die is noted.
(a) Create a probability distribution for the number displayed on the top face of the die.
(b) Determine the expected value for the number displayed on the top face of the die.
2. A pair of fair dice is rolled. The number (of dots) displayed on the top face of each die is noted.
(a) Create a probability distribution for sum of the numbers displayed on the top face of each die.
(b) Determine the expected value for the sum of the numbers displayed on the top face of each die.
3. Create a probability distribution for the toss of a fair coin.
4. Create a probability distribution for the number heads for the toss of a fair coin.
5. Create a probability distribution for the number of heads for the toss of two fair coins.
6. Create a probability distribution for the number of tails for the toss of three fair coins.
7. A raffle has four prizes, a first prize of $\$ 500$, a second prize of $\$ 200$, two third prizes of $\$ 50$ each, and three fourth prizes of $\$ 10$ each. Suppose 1000 tickets are sold for $\$ 1$ each.
(a) Create a probability distribution for the prize that someone who buys one ticket may win.
(b) Create a probability distribution for the possible winnings for someone who buys one ticket.
(c) Determine the expected prize for someone who buys one ticket.
(d) Determine the expected winnings for someone who buys one ticket.
8. A raffle has a $\$ 1000$ grand prize as well as four other types of prizes, a first prize of $\$ 500$, two second prizes of $\$ 200$, three third prizes of $\$ 75$ each, and four fourth prizes of $\$ 25$ each. Suppose 10,000 tickets are sold for $\$ 5$ each.
(a) Create a probability distribution for the prize that someone who buys one ticket may win.
(b) Create a probability distribution for the possible winnings for someone who buys one ticket.
(c) Determine the expected prize for someone who buys one ticket.
(d) Determine the expected winnings for someone who buys one ticket.
